

## HPF Implementation of NPB2.3

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### Abstract

We present an HPF implementation of BT, SP, LU, FT, CG and MG of NPB2.3-serial benchmark set. The implementation is based on HPF performance model of the benchmark specific primitive operations with distributed arrays. We present profiling and performance data on SGI Origin 2000 and compare the results with NPB2.3. We discuss an advantages and limitations of HPF and pghpf compiler.

### 1. Introduction

The goal of this study is an evaluation of High Performance Fortran (HPF) as a choice for machine independent parallelization of aerophysics applications. These applications can be characterized as numerically intensive computations on a set of 3D grids with local access patterns to each grid and global synchronization of boundary conditions over the grid set. In this paper we limited our study to six NAS benchmarks: simulated applications BT, SP, LU and kernel benchmarks FT, CG and MG, [2].

HPF provides us with a data parallel model of computations [8], sometimes referred also as SPMD model [12]. In this model calculations are performed concurrently with data distributed across processors. Each processor processes the segment of data which it owns. The sections of distributed data can be processed in parallel if there are no dependencies between them.

The data parallel model of HPF appears to be a good paradigm for aerophysics applications working with 3D grids. A decomposition of grids into independent sections of closely located points followed by a distribution of these sections across processors would fit into the HPF model. In order to be processed efficiently these sections should be well balanced in size, should be independent and should be regular. In our implementation of the benchmarks we addressed these issues and suggested data distributions satisfying these requirements.

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HPF has a limitation in expressing pipelined computations which are essential for parallel processing of distributed data having dependencies between sections. This limitation obliges us to keep a scratch array with an alternate distribution and redistribute codependent data onto the same processor to perform parallel computations (see sections on BT, SP and FT).

A practical evaluation of the HPF versions of benchmarks was done with the Portland Group `pgHPF 2.4` compiler [12] on SGI Origin 2000 (the only HPF compiler available to us at the time of writing). In the course of the implementation we had to address several technical problems: overhead introduced by the compiler, unknown performance of operations with distributed arrays, additional memory required for storing arrays with an alternative distribution. To address these problems we built an empirical HPF performance model, see Section 3. In this respect our experience confirms two known problems with HPF compilers [11],[4]: lack of theoretical performance model and the simplicity of overlooking programming constructs causing poor code performance. A significant advantage of using HPF is that the conversion from F77 to HPF results in a well structured easily maintained portable program. An HPF code can be developed on one machine and ran on another (more then 50% of our development was done on NAS Pentium cluster Whitney).

In section 2 we consider a spectrum of choices HPF gives for code parallelization and build an empirical HPF performance model in section 3. In section 4 we characterize the algorithmic nature of BT, SP, LU, FT, CG and MG benchmarks and describe an HPF implementation each of them. In section 5 we compare our performance results with NPB2.3. Related work and conclusions are discussed in section 6.

## 2. HPF Programming Paradigm

In the data parallel model of HPF calculations are performed concurrently over data distributed across processors\*. Each processor processes the segment of data which it owns. In many cases HPF compiler can detect concurrency of calculations with distribut-

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\*The expression "data distributed across processors" commonly used in papers on HPF is not very precise since data resides in memory. This expression can be confusing for shared memory machine. The use of this expression assumes that there is a mapping of memory to processors.

ed data. HPF advises a two level strategy for data distribution. First, arrays should be coaligned with ALIGN directive. Then each group of coaligned arrays should be distributed onto abstract processors with the DISTRIBUTE directive.

HPF has several ways to express parallelism: f90 style of array expressions, FORALL and WHERE constructs, INDEPENDENT directive and HPF library intrinsics [9]. In array expressions operations are performed concurrently with segments of data owned by a processor. The compiler takes care on communicating data between processors if necessary. FORALL statement performs computations for all values of the index (indices) of the statement without guarantying any particular ordering of the indices. It can be considered as a generalization of f90 array assignment statement.

INDEPENDENT directive states that there is no dependencies between different iterations of a loop and the iterations can be performed concurrently. In particular it asserts that Bernstein's conditions are satisfied: set of read and written memory locations on different loop iterations don't overlap and no memory location is written on different loop iterations, see [8], p. 193. All loop variables which do not satisfy the condition should be declared as new and are replicated by the compiler in order the loop to be parallelized.

Many HPF intrinsic library routines work with arrays and are executed in parallel. For example, random\_number subroutine initializes an array of random numbers in parallel with the same result as a sequential subroutine compute\_initial\_conditions of FT. Other examples are intrinsic reduction and prefix functions.

### **3. Empirical HPF Performance Model**

The concurrency provided by HPF does not come for free. The compiler introduces overhead related to processing of distributed arrays. There are several types of the overhead: creating communication calls, implementing independent loops, creating temporaries and accessing distributed arrays elements. The communication overhead is associated with requests of elements residing on different processors when they are necessary for evaluation of an expression with distributed arrays or executing an iteration of an independent loop. Some communications can be determined in the compile time other can be determined only in run time causing extra copying and scheduling of communi-

cations, see [12], section 6. As an extreme case the calculation can be scalarized and result in a significant slowdown.

The implementation of independent loops in `pghpf` is based on assignment of a home array to each independent loop that is an array relative to which loop iterations are localized. The compiler selects a home array from array references within the loop or creates a new template for the home array. If there are arrays which are not aligned with the home array they are copied into a temporary array. It involves allocating/deallocating of the temporaries on each execution of the loop. A additional overhead associated with the transformations on the loop which the compiler has to perform to ensure its correct parallel execution.

Temporaries can be created when passing a distributed array to a subroutine. All temporarily created arrays must be properly distributed to reduce the amount of the copying. Inappropriate balance of the computation/copy operations can cause noticeable slowdown of the program.

The immanent reason of the overhead is that HPF hides the internal representation of distributed arrays. It eliminates the programming effort necessary for coordinating processors and keeping distributed data in a coherent state. The cost of this simplification is that the user does not have a consistent performance model of concurrent HPF constructs. The `pghpf` compiler from Portland Group has a number of ways to convey the information about expected and actual performance to the user. It has flags `-Minfo` for the former, `-Mprof` for the later and `-Mkeepftn` for keeping the intermediate FORTRAN code for the user examination. The `pghpf` USER's guide partially addresses the performance problem by a partial discloser of the implementation of the INDEPENDENT directive and of distributed array operations, cf. [12], Section 7.

To compensate for lack of a theoretical HPF performance model and to quantify compiler overhead we have built an empirical performance model. We have analyzed NPB, compiled a list of array operations used in the benchmarks and then extracted a set of primitive operations upon which they can be implemented. We measured performance of the primitive operations with distributed arrays and used the results as a guide in HPF implementations of NPB.

We distinguish 5 types of primitive operations with distributed arrays, as summa-

rized in Table 1:

- loading/storing a distributed array and copying it to another distributed array with the same or a different distribution (includes shift, transpose and redistribution operations),
- filtering a distributed array with a local kernel (the kernel can be first or second order stencil as in BT, SP and LU or 3x3x3 kernel of the smoothing operator as in MG),
- matrix vector multiplication of a set of 5x5 matrices organized as 3D array by a set of 5D vectors organized in the same way (manipulation with 3D arrays of 5D vectors is a common CFD operation),
- passing a distributed array as an argument to a subroutine,
- performing a reduction sum.

We used 5 operations of the first group including: (1) assignment values to a nondistributed array, (2) assignment values to a distributed array, (3) assignment values to a distributed array with a loop along a nondistributed dimension declared as independent, (4) shift of a distributed array along a distributed dimension and (5) copy of a distributed array to an array distributed along another dimension (redistribution). In the second group we used filtering with the first order (4 point) finite difference stencil and the second order (7 point) finite difference stencil. We used both the loop syntax and the array syntax for implementation. In the third group we used 2 variants of matrix vector multiplication: (10) the standard and (11) with the internal loop unrolled. In the fourth group we have passed 2D section of 5D array to a subroutine. (This group appeared to be very slow and we did not include it into the table). The last group includes: (12) reduction sum of a 5D array to a 3D array and (13) reduction sum.

All arrays in our implementations of these primitive operations are 101x101x101 arrays (odd block sizes were chosen to reduce the cash related effects) of double precision numbers, 5D vectors and of 5x5 matrices. We used BLOCK distribution only. The profiling results of these operations, compiled with `pghpf` and ran on SGI Origin 2000, are given in the Table 1. The execution time of the first operation compiled for single processor was chosen as a base time in each group.

We can suggest some conclusions from the profiling data.

- Execution of a sequential code slows down as the number of processors grows (line 1).
- Distribution of an array can have a significant penalty (f90 vs. column 1). For example INDEPENDENT directive causes the loop to be compiled for symbolic number of processors and the its bounds have to be localized causing some overhead.
- An inappropriate placement of independent directive confuses the compiler and slows down the program (line 3).
- Efficiency of some parallel operations is close to 1 (lines 6 and 11) while other have efficiency less then 0.5 (lines 2 and 4).
- Replacing loops with array assignment speeds up the sequential program (line 7 and 9 vs. line 6 and 8) but has no effect on parallel performance. Warning: pghpf does not parallelize independent loops with nonelemental assignments.
- loop unrolling does not effect performance (line 11 vs. line 10). In pghpf 2.2 the difference was larger than a factor of 3 for more than 8 processors.
- The smaller number of dimensions are reduced the better scales the operation (line 12 vs. line 13)
- Passing array sections as arguments are an order of magnitude slower then passing the whole array (not included in the table).

We have used the model to choose the particular way to implement operations with distributed arrays. For example, we have used an array syntax instead of loops in the cases where communications were required (such as calculating differences along the distributed direction). Also we have inlined subroutines called inside of loops with sections of distributed arrays as arguments. We have parallelized a loop even if it looked like the loop performs a small amount of computations and should not effect the total computation time (see conclusion 1).

Operation Name\procs	Single Proc	1	2	4	8	16	32
1. Serial assignment	1.00	1.27	1.37	1.52	1.56	2.99	3.06
2. Distributed assignment	1.23	1.27	0.68	0.37	0.18	0.10	0.04
3. Distributed assignment + INDEPENDENT	0.89	8.82	5.44	2.89	1.24	0.90	0.58
4. Distributed shift	1.34	2.59	1.93	1.10	0.69	0.65	0.62
5. Redistribution	1.34	1.00	1.21	0.93	0.41	0.30	0.24
6. First order stencil sum	1.00	1.55	0.77	0.24	0.10	0.05	0.03
7. First order stencil sum (array syntax)	0.72	1.55	0.80	0.24	0.09	0.05	0.03
8. Second order stencil sum	1.09	1.94	0.97	0.34	0.14	0.07	0.03
9. Second order stencil sum (array syntax)	0.85	2.18	1.05	0.38	0.16	0.07	0.03
10. Matrix vector multiplication	1.00	1.45	0.67	0.43	0.13	0.11	0.05
11. Matrix vector mult. with internal loop unrolled	1.23	1.49	0.69	0.44	0.14	0.11	0.05
12. 5D to 3D reduction sum	1.00	1.44	0.77	0.42	0.22	0.15	0.06
13. Reduction sum	9.83	2.19	1.16	0.60	0.39	0.19	0.10

**TABLE 1.** Relative time of basic operations on SGI Origin 2000. The column labeled as "Single Proc" lists the results of the program compiled with a flag -Mf90 and ran on a single processor. This removes overhead of handling of distributed arrays. All other columns list results of the program compiled for a symbolic number of processors and ran on the specified number of processors.

We used pgprof and internal NPB timer for profiling the code. The pgprof allows to

display time spent in subroutines or lines of the code per each processor. To get the profiling data the code should be compiled with `-Mprof=lines` or `-Mprof=func` flag. The profiler also allows to display the number and the total size of messages. The profiling involves a significant overhead and can not be used for profiling of large programs. For profiling of the benchmarks we used internal timer supplied with NPB. The timer is serial and can be accessed at synchronization points only which makes it unsuitable for a fine grain profiling such as processor load variation.

#### **4. HPF Implementation of NAS Benchmarks**

NAS Parallel Benchmarks consist of eight benchmark problems (five kernels and three simulated CFD applications) derived from important classes of aerophysics applications [2]. The NPB2.3 suite contains MPI implementation of the benchmarks which have good performance on multiple platforms and are considered as a reference implementation. The NPB2.3-serial suite is intended to be starting points for the development of both shared memory and distributed memory versions, for the testing parallelization tools, and also as single processor benchmarks. We have not included HPF version of EP since we don't expect to get any useful data on HPF performance from EP. We have not included HPF version of C benchmark IS either as well.

We took NPB2.3-serial as a basis for HPF version. We used our empirical HPF performance model as a guide for achieving performance of HPF code. Also we relied on the compiler generated messages regarding the information on loop parallelization and warnings about expensive communications. We used standard HPF directives (actually a very limited basic subset of the directives) as specified in [7].

We limited ourselves with moderate modifications of the serial versions such as inserting HPF directives, writing interfaces, interchanging loops and depth-1 loop unrolling. In a sense the resulting code is f77, code modernized with f90 syntax and HPF directives rather than pure HPF code. We avoided significant changes such as inlineing, removing arrays from common blocks and passing them as subroutines arguments. We avoided usage of optimized low level linear algebra and FFT library subroutines. In our explanation of the code we refer to NPB2.3-serial FORTRAN code.



The source code of NPB can be found in NAS parallel benchmarks home page <http://science.nas.nasa.gov/Software/NPB>. The page also contains links to HPF implementations of NPB by Portland Group and by Advanced Parallel Research. An extensive data on NPB performance can be found in T. Faulkner's home page: <http://science.nas.nasa.gov/~faulkner>. A comparison of different approaches to parallelization of NPB is given in [5].

Benchmarks BT, SP and LU are solving a 3D discretization of Navier-Stokes equation

$$Ku = r \quad (1)$$

where  $u$  and  $r$  are 5D vectors defined in the points of 3D rectangular grid and  $K$  is a 7 diagonal block matrix of 5x5 blocks. The three benchmarks differ in splitting the matrix  $K$ . The FT performs FFT of a 3D array, CG solves a sparse system of linear equations by the conjugated gradient method, and MG solves a discrete Poisson problem on a 3D grid by the  $V$ -cycle multigrid algorithm.

#### 4.1 BT Benchmark

BT uses Alternating Direction Implicit (ADI) approximate factorization of the operator of equation (1):

$$K \cong BT_x \cdot BT_y \cdot BT_z$$

where  $BT_x$ ,  $BT_y$  and  $BT_z$  are block tridiagonal matrices of 5x5 blocks if grid points are enumerated in an appropriate direction. The resulting system then solved by solving the block tridiagonal systems in  $x$ -,  $y$ - and  $z$ -directions sequentially. The main iteration loop of BT starts from the computation of  $r$  (`compute_rhs`) followed by sequential inversion of  $BT_x$ ,  $BT_y$  and  $BT_z$  (`x_solve`, `y_solve` and `z_solve`) and is concluded with updating of the main variable  $u$  (`add`).

Each subroutine `x_solve`, `y_solve` and `z_solve` solves a second order recurrence in the appropriate direction. These computations can be done concurrently for all grid lines parallel to an appropriate axis while the computation along each line is sequential. A concurrency in `x_solve` and `y_solve` can be achieved by distributing the grid along  $z$ -direction. This distribution, however, would preclude concurrency in `z_solve`

since HPF can not organize processors to work in a pipelined mode. In order for `z_solve` to work in parallel the grid has to be redistributed along  $x$ - or  $y$ -direction or both.

In our HPF implementation of BT the subroutines `compute_rhs`, `x_solve`, `y_solve` and `add` work with `u`, `rhs` and `lhs` distributed blockwise along  $z$ -direction. The subroutine `z_solve` works with `rhsz` and `lhsz` distributed blockwise along  $y$ -direction. The redistribution of `rhs` to `rhsz` is performed at the entrance to `z_solve` and back redistribution is performed upon exit from `z_solve`. The redistribution `uz=u` performed just before calculation of `lhsz`.

The main loop in `x_solve` (symmetrically `y_solve` and `z_solve`) for each grid point calls  $5 \times 5$  matrix multiplication,  $5 \times 5$  matrix inversion and  $5 \times 5$  matrix by 5 dimensional vector multiplication. Using `pgprof` we found that the calls had generated too much overhead probably related to passing a section of a distributed array to a subroutine. These subroutines were inlined and the external loop was unrolled. This reduced the execution time by a factor of 2.9 on up to 8 processors. For a larger number of nodes scaling comes into effect and reduction is less.

The inlining and loop unrolling made internal loop of `x_solve` too complicated and the compiler message indicated that it was not been able to parallelize the loop. The `INDEPENDENT` directive was sufficient for parallelization of the loop, however it introduced an overhead which caused the program run 1.85 times slower on single processor relative to the program compiled with `-Mf90` flag.

Note that two dimensional distributions of `gridz` and/or `gridy` would not give any reduction in computation to communication ratio. Opposite, it would require to redistribute data three times per iteration and would resulted in a slower program.

The profile of main BT subroutines is shown on Figure 1. The subroutines which not involve redistribution and/or communications scale down nicely. The communication during the computations of fluxes and dissipation in  $z$ -direction effects scaling of `rhs`. The redistribution time essentially stays constant with the number of processors and is responsible for dropping of the efficiency for more then 8 processors.

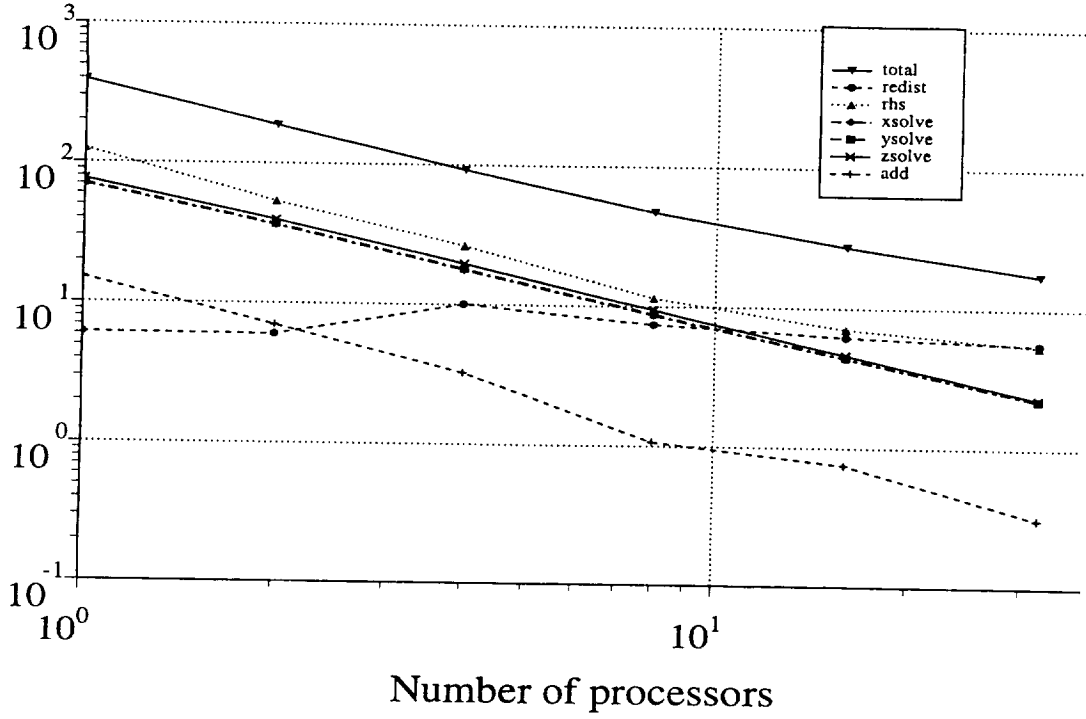


FIGURE 1. BT profile on Origin 2000. Note that rhs does not scale well since it involves communications when computing the flux and the dissipation in z-direction. The redistribution diminishes the efficiency of the processors utilization as the number of processors grows.

#### 4.2 SP Benchmark

SP uses the Beam-Warming approximate factorization of the operator of equation (1):

$$K \cong T_x \cdot P_x \cdot T_x^{-1} \cdot T_y \cdot P_y \cdot T_y^{-1} \cdot T_z \cdot P_z \cdot T_z^{-1}$$

where  $T_x$ ,  $T_y$  and  $T_z$  are block diagonal matrices of 5x5 blocks,  $P_x$ ,  $P_y$  and  $P_z$  are block pentadiagonal matrices of 5x5 diagonal blocks. The resulting system then solved by inverting block diagonal matrices  $T_x$ ,  $T_x^{-1} \cdot T_y$ ,  $T_y^{-1} \cdot T_z$  and  $T_z^{-1}$  and solving the block pentadiagonal systems.

The main iteration loop of SP is similar to one of BT. It starts with the computation of rhs which is almost identical to compute\_rhs in BT followed by the interleaved inver-

sion of block diagonal and block pentadiagonal matrices and is concluded with updating of the main variable  $u$  (add). The main iteration loop of SP is shown in Figure 2.

```

do step = 1,niter
  call compute_rhs
  call txinvr
  call x_solve
  call ninvr
  call y_solve
  call pinvr
  call z_solve
  call tzetar
  call add
end do

```

FIGURE 2. The main iteration loop of SP

Parallelization of SP is similar to the parallelization of BT: all subroutines except `z_solve` operate with data distributed blockwise along  $z$ -direction. The subroutine `z_solve` works with data distributed blockwise along  $y$ -direction. The redistribution of `rhs` and of few auxiliary arrays is performed at the entrance to `z_solve` and back redistribution of `rhs` is performed on the exit from `z_solve`. As in BT a 2D distributions would require more redistributions and would slow down the benchmark.

Profile of SP (see Figure 3) suggests few conclusions. The dominant factor of the computing time is the computation of `rhs` and the redistribution. The redistribution time vary slightly with the number of processors and is the major factor effecting scaling of the benchmark. The communications involved in compute `rhs` in  $z$ -direction also effect the scaling. The solution of the system takes much less time than these two operations and scales well.

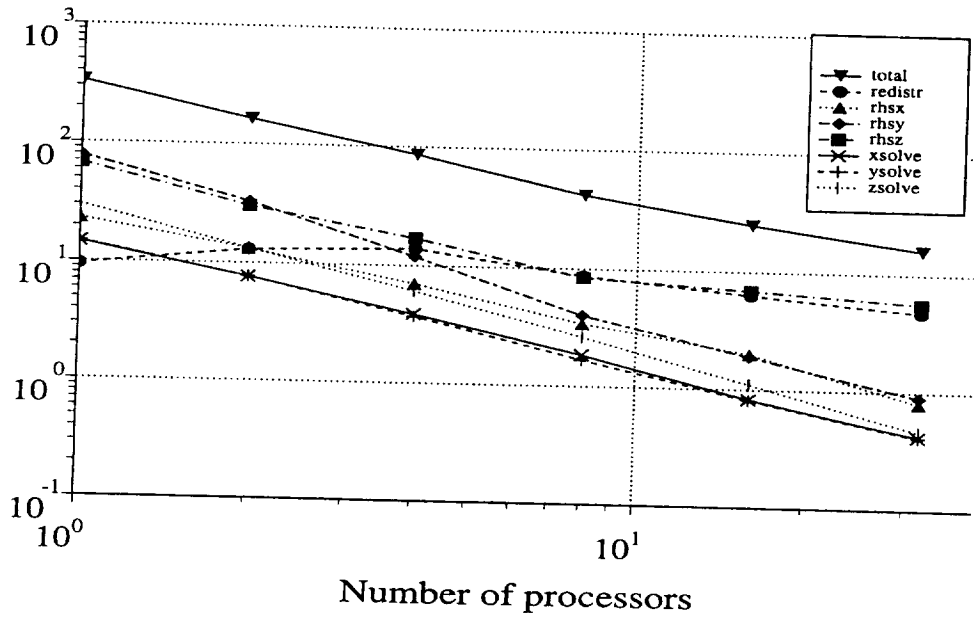


FIGURE 3. SP profile on SGI Origin 2000. The redistribution and communications in rhsz effect scaling of SP.

#### 4.3 LU Benchmark

LU implements a version of SSOR algorithm by splitting of the operator of equation (1) into a product of lower triangular matrix and upper triangular matrix:

$$K \equiv \omega(2 - \omega)(D + \omega Y)(I + \omega D^{-1}Z)$$

where  $\omega$  is a relaxation parameter,  $D$  is the main block diagonal of  $K$ ,  $Y$  is three sub block diagonals and  $Z$  is three super block diagonals. The system is solved by computing of elements of the triangular matrices (subroutines jacld and jacu) and solving the lower and the upper triangular system (subroutines blts and buts).

The ssor is implemented as a sequence of sweeping of the horizontal planes of the grid, see Figure 4.

```

DO k = 2, nz -1
  call jacld(k)
  call blts(k)
END DO
DO k = nz - 1, 2, -1
  call jacu(k)
  call buts(k)
END DO
call add
call rhs

```

**FIGURE 4.** SP implementation of `ssor` subroutine.

The subroutines `jacld`, `jacu`, `add` and `rhs` are completely parallel meaning that operations can be performed concurrently in all grid points. Both `blts` and `butts` have a limited parallelism because processing of an  $(i,j,k)$  grid point depends on the values in the points  $(i+e,j,k)$ ,  $(i,j+e,k)$  and  $(i,j,k+e)$ , where  $e = -1$  for `blts` and  $e = 1$  for `butts`. The small amount of work on each parallel step would cause too many messages to be sent. A method of increasing parallelism and of reduction of the number of messages is given in Hyperplane Algorithm [3] and we decided to choose this algorithm for HPF implementation.

In the Hyperplane Algorithm computations are performed along the planes  $i+j+k=m$ , where  $m$  is plane number,  $m = 6, \dots, nx+ny+nz-3$ . For calculation of the values on each plane values from the previous plane (lower triangular system) or from the next plane (upper triangular system) are used.

In the Hyperplane Algorithm the external loop on  $k$  was replaced by the loop on the plane number  $m$ , and  $j$ -loop bounds became functions of  $m$  and  $i$ -loop bounds became functions of  $m$  and  $j$  and  $k$  is computed as  $k = m-i-j$ . These loop bounds were taken from precalculated arrays.

Parallelization of LU was done by distribution of arrays blockwise along  $j$ -direction. An advantage of LU relative to BT and SP is that no redistributions are necessary. A disadvantage is that plane grid points are distributed not evenly across processors causing load imbalance. A 2D distribution could not be handled by the compiler efficiently. (The problem was in assigning of an appropriate home array to a nest of two independent loops with variable loop bounds.)

Profile of LU is shown in Figure 5. Low efficiency of LU resulted from two sources: a

large number of relatively small messages have to be sent after each iteration of  $m$  loop, and a poor load balancing.

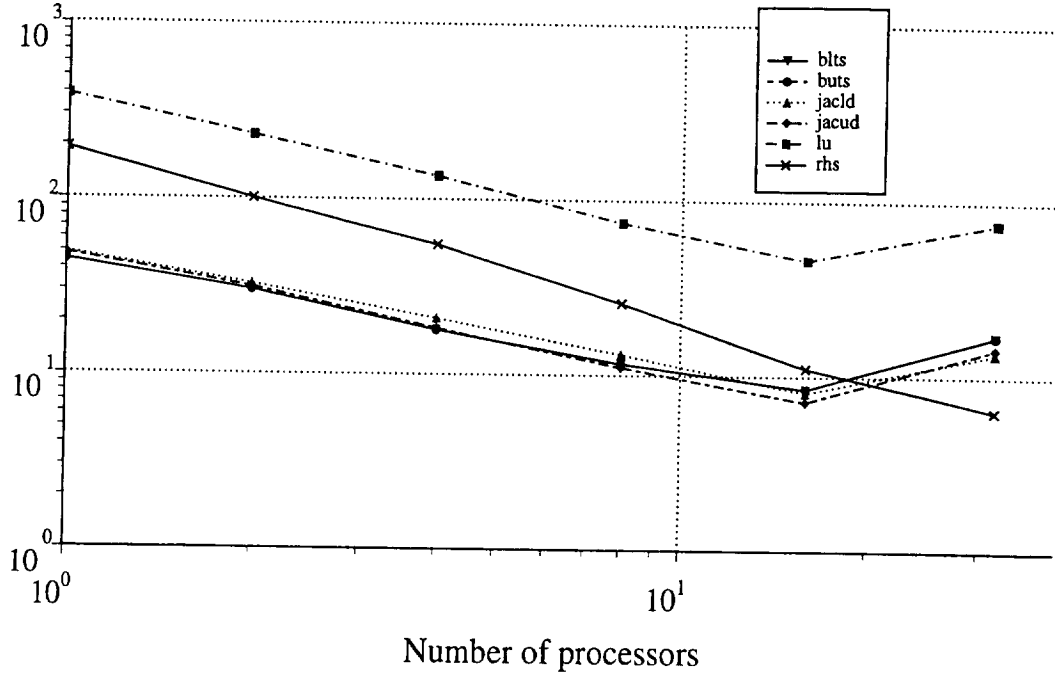


FIGURE 5. LU profile on SGI Origin 2000

#### 4.4 FT Benchmark

FT implements FFT of a 3D array. The transformation can be formulated as a matrix vector multiplication:

$$v = (F_m \otimes F_n \otimes F_k)u$$

where  $u$  and  $v$  are 3D arrays of dimensions  $(m,n,k)$  represented as vectors of dimensions  $m \times n \times k$  and  $F_l, l=m,n,k$  is an FFT matrix of the order  $l^*$ . The algorithm is based on factorization of the FFT matrix:

$$F_m \otimes F_n \otimes F_k = (I_m \otimes I_n \otimes F_k)(I_m \otimes F_n \otimes I_k)(F_m \otimes I_n \otimes I_k)$$

where  $I_l, l=m,n,k$  is the identity matrix of the order  $l$ . Multiplication of each factor by a vector is equivalent to FFT of the array in one dimension, henceforth FT performs FFTs in

\* Here  $A \otimes B$  is a block matrix with blocks  $a_{ij}B$  and is called a tensor product of  $A$  and  $B$

$x$ -,  $y$ - and  $z$ - directions successively. The core FFT in one direction is implemented as a Shwarztrauber's vectorization of Stockham autosorting algorithm performing independent FFTs over sets of vectors. The number of vectors in the sets are chosen to fit the sets into the primary cash of the Origin 2000.

For HPF implementation we distributed  $u$  blockwise in  $z$ -direction, perform FFTs in  $x$ -direction, transpose the array, perform FFT in  $y$ -direction, redistribute the array along  $y$ -direction and perform FFT in  $z$ -direction. The loops with FFTs in one direction calling pure Swarztrauber subroutine were declared as INDEPENDENT. The transposition and redistribution operations were converted by pghpf compiler to FORALL statements automatically given -Mautopar flag so that INDEPENDENT directives were unnecessary for these loops.

Note the significant difference between transposition and redistribution. The transposition operation involves reading an array columnwise and writing it rowwise and assumes that these dimensions are not distributed. The transposition does not involve communications. The redistribution copies between two arrays with different distributions and usually requires all-to-all communications. The difference between transposition and redistribution is not as significant on shared memory machines as on distributed memory machines.

Note also that iterations of FT are independent since the result of one iteration is not used for the next one. Neither our HPF version of FT nor NPB2.3 version take the advantage of this level of parallelism.

Profile of FT, see Figure 6, shows that the core FFT computations consume about 50% of total time and scale down well with the number of processors. The redistribution and transposition don't scale down as consistent as the core calculations reducing the efficiency of the benchmark on large number of processors.



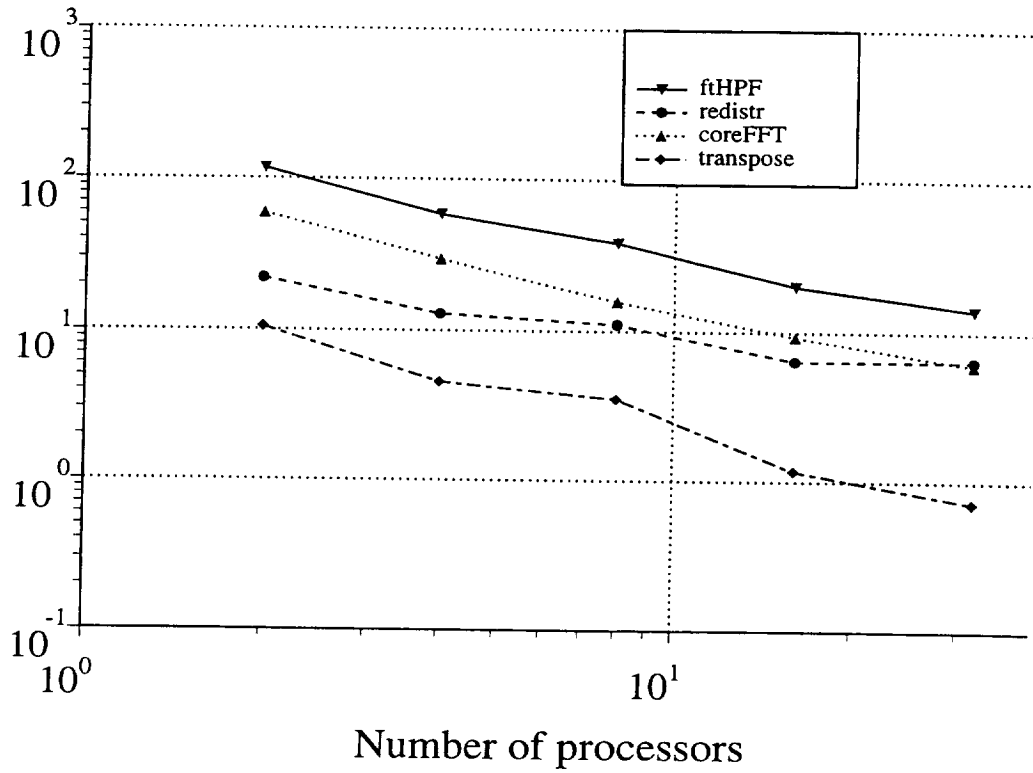


FIGURE 6. FT profile on SGI Origin 2000.

#### 4.5 CG Benchmark

CG is different from the other benchmarks since it works with a large sparse unstructured matrix. CG estimates the largest eigenvalue of a symmetric positive definite sparse matrix by the inverse power method. The core of CG is a solution of sparse system of linear equations by iterations of the conjugate gradient method:

$$q = Ap, \quad d = p^T q$$

$$\alpha = \frac{\rho}{d}, \quad z = z + \alpha p, \quad r = r - \alpha q$$

$$\rho_0 = \rho, \quad \rho = r^T r, \quad \beta = \frac{\rho}{\rho_0}, \quad p = r + \beta p$$

The main iteration loop contains one sparse matrix vector multiplication, two reduc-

tion sums, three daxpy operations and a few scalar operations. The most expensive operation of the algorithm is the sparse matrix vector multiplication  $q = Ap$ . Nonzero elements of  $A$  are stored row by row in a compressed format. The column indices of matrix elements are stored in a separate array `colidx`.

The matrix vector multiplication and daxpy operations are parallel. In our HPF implementation we distribute  $z, q, r$ , and  $x$  and replicate  $A, p$  and `colidx`. It allowed to perform matrix vector operation in parallel, however the daxpy operations were performed with vectors having different distributions. This distribution gave us the best performance results of all other distributions we have tried.

The replication of  $A$  will cause problems if  $A$  will not fit into memory of one processor. On each processor only a small number of rows of  $A$  are used to calculate the section of  $q$  distributed onto the processor. The sparsity of  $A$  makes the sizes of the rows vary and in order to distribute it we created a matrix  $B$  with number of columns equal to the maximum number of nonzero elements in rows of  $A$ . We aligned rows of  $B$  with  $q$  and copied  $A$  to  $B$  row by row. This eliminated replication of  $A$ , however resulted in 20% slower code.

The profile of CG is shown in Figure 7. The matrix vector multiplication scales down well. The daxpy operations of a replicated  $p$  with distributed vectors  $r$  and  $z$  scale up distorting performance on 32 processors. An explicit replication of  $p$  slows the program down. An algorithm for matrix vector multiplication which does not require a redistribution is given in [10]. This algorithm communicates partial sums of the matrix vector product according to a special schedule which can not be expressed in HPF.

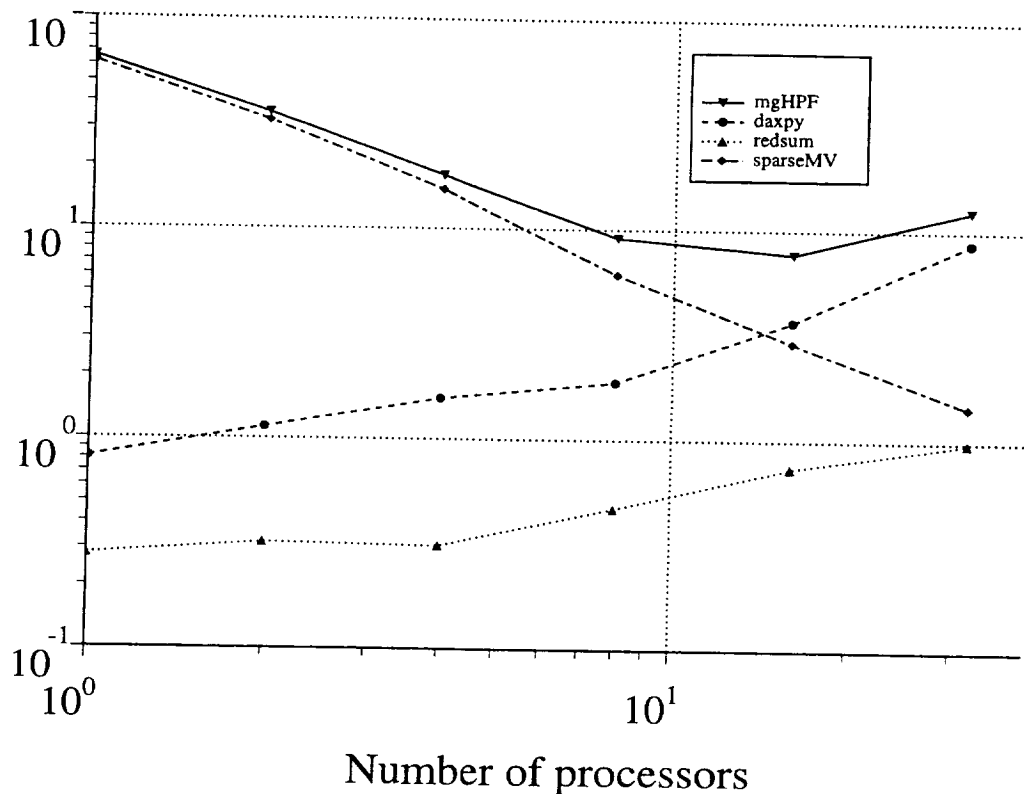


FIGURE 7. CG profile on SGI Origin 2000

#### 4.6 MG benchmark

MG benchmark performs iterations of V-cycle multigrid algorithm for solving a discrete Poisson problem  $\nabla u = v$  on a 3D grid with periodic boundary conditions [2]. Each iteration consists of evaluation of the residual:

$$r = v - Au$$

and of the application of the correction:

$$u = u + Mr$$

where  $M$  is the V-cycle multigrid operator.

The V-cycle starts from a solution on the finest grid, computes the residual and projects it onto more and more coarse grids (down step). On the coarsest grid it computes an approximate solution by smoothing the residual (psinv subroutine), interpolates the

solution onto a finer grid, computes the residual and applies the smoothing on the finer grid (up substep). In a few `interp-resid-psinv` substeps the V-cycle finishes with an updated solution on the finest grid.

To implement MG in HPF we introduced a 4 dimensional array and mapped grids into 3D sections of this array with a fixed value of the last dimension. We used 1D BLOCK distribution of the array in z-direction. The projection, interpolation, smoothing and computation of the residual act at each grid point independently. 2D or 3D partitions would reduce the number of cuts in the array and would reduce the number of messages. On practice, however 2D partition resulted in a slightly slower code and 3D partition in a significantly slower code.

The HPF implementation of MG stretches the limits of `pghpf` in few respects. First, the number of grids and their sizes vary depending on the benchmark class. In order to be able to implement a loop over the grid we need an array of pointers to arrays. This feature is not implemented in the version of `pghpf` compiler which we used. As a work around we introduced the 4D array and used its last dimension as a grid pointer. The overhead of this is allocation of significantly larger memory than actually is used. (In the original `f77` version 3d arrays are packed into a 1D array and are referred to by the address of the first elements.)

Second, the residual and the smoother subroutines work on the same grid performing convolutions with  $3 \times 3 \times 3$  kernels. This operation requires access to non local sections of data and results in a poor scalability of these two subroutines, see MG profile on Figure 9. We tried to use an array syntax for implementation of these convolutions but could not get any speed up.

The projection and the interpolation subroutines work with a pair of grids one of which is a refinement of another. Using the same block distribution for all grids collapses the coarsest grids onto a smaller number of processors. It inhibits access to the appropriate portions of the coarser grid. The projection and the interpolation subroutines involve

the shuffling operations with grids:

$$\begin{aligned} u(2*i1-1, 2*i2-1, 2*i3-1) &= u(2*i1-1, 2*i2-1, 2*i3-1) + \\ & \quad z(i1, i2, i3) \\ u(2*i1, 2*i2-1, 2*i3-1) &= u(2*i1, 2*i2-1, 2*i3-1) + \\ & \quad z(i1+1, i2, i3) + z(i1, i2, i3) \end{aligned}$$

The compiler was not able to parallelize the loop with the shuffling operation in the body because of complex index expressions (according to the compiler's message). We have used the array syntax and ONHOME clause for parallelization, see Figure 8.

```
!hpf$ align w011(i1,i2,i3) with u(2*i1,2*i2-1,2*i3-1)
!hpf$ align w111(i1,i2,i3) with u(2*i1-1,2*i2-1,2*i3-1)
w111(1:mm1-1,1:mm2-1,1:mm3-1) = z(1:mm1-1,1:mm2-1,1:mm3-1)
w011(1:mm1-1,1:mm2-1,1:mm3-1) =
> z(1:mm1-1,1:mm2-1,1:mm3-1) + z(2:mm1,1:mm2-1,1:mm3-1)
!hpf$ independent, on home(w011(i1,i2,i3))
do i3=1,mm3-1
do i2=1,mm2-1
do i1=1,mm1-1
u(2*i1,2*i2-1,2*i3-1) = u(2*i1,2*i2-1,2*i3-1)+w011(i1,i2,i3)
end do
end do
end do
!hpf$ independent, on home(w111(i1,i2,i3))
do i3=1,mm3-1
do i2=1,mm2-1
do i1=1,mm1-1
u(2*i1-1,2*i2-1,2*i3-1) = u(2*i1-1,2*i2-1,2*i3-1)+w111(i1,i2,i3)
end do
end do
end do
```

**FIGURE 8.** Implementation of the shuffling with on HOME clause

The profile of MG (see Figure 9) shows that the smoothing and the residual operators are not scaled well. These operators are not factored and require communications to access grid points distributed on different processors.

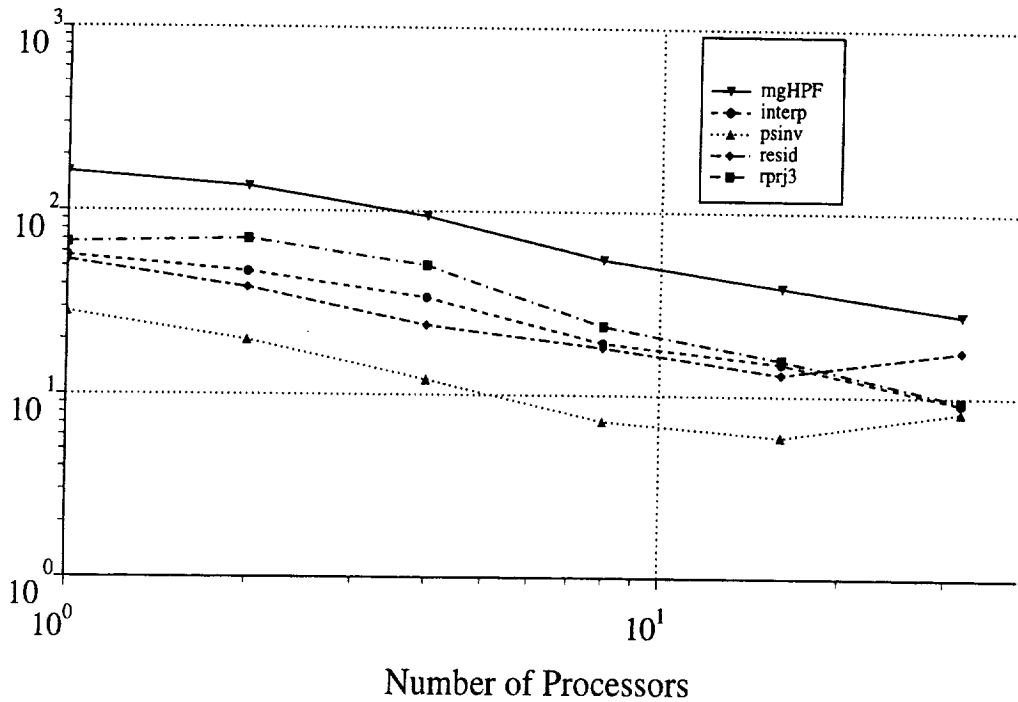


FIGURE 9. MG profile on SGI Origin 2000

## 5. Comparison with MPI version of NPB2.3

The timing results of the benchmarks are summarized in Table 2 and the plot is shown in Figure 10. As a reference we use time of the MPI version reported on NPB home page. The HPF version is consistently slower than MPI version. The lower performance of HPF versions results from two main sources: a single node code HPF code runs slower and it does not scale as well as MPI code.

A comparison of single process performance of `pgHPF` compiled code versus `f77` code shows that former generates about 2 times slower code than latter. Since we did not do any code modifications which would change the total operations count or would distort any array layout in the memory (MG is an exclusion), we would account this slowdown to the compiler introduced overhead and cost of the redistribution. (The redistribution on single processor consumes less than 10% of the computational time.)

Processor utilization in HPF code is not as efficient as in MPI versions (NPB 2.3) for two reasons. HPF versions require an extra redistribution of big arrays and the redistri-

bution does not scale down well. In the version of the compiler which we had the REDISTRIBUTE statement had not been implemented. Implementation of this directive would allow to organize computations in BT and SP in the following sequence

x\_solve, y\_solve, z -> y redistribution, z\_solve,

x\_solve, y -> x redistribution, y\_solve, z\_solve, x -> z redistribution, ...

This would require 3 redistributions per 2 iterations instead of current 4 and would reduce redistribution overhead by a factor of 3/4. The redistribution was the main reason of flattening performance between 16 and 32 processors in BT, SP and FT. An efficient implementation of redistribution would improve scalability of these benchmarks. In the HPF 2.0 language specification, however, the status of REDISTRIBUTE was changed from the language statement to an approved extension, see [7], probably because of difficulties with the implementation.

**TABLE 2. Benchmarks time on SGI Origin 2000(sec)**

<b>Nprocs</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>	<b>9</b>	<b>16</b>	<b>25</b>	<b>32</b>
BT.A pghpf 2.4	3911.3	1865.4	921.1	469.7		273.6		174.0
BT.A NPB2.3	2611.0		731.5		314.0	161.4	91.9	
SP.A pghpf 2.4	3302.9	1629.4	861.2	416.1	371.6	248.4	175.7	158.9
SP.A NPB2.3	1638.4		352.6		142.0	79.1	46.2	
LU.A pghpf 2.4	3285.2	2277.8	1350.4	752.7		462.4		755.6
LU.A NPB2.3	1741.5	795.0	308.2	144.3		67.4		33.8
FT.A pghpf 2.4		116.8	58.1	38.1		20.1		14.0
FT.A NPB2.3	132.8	85.8	44.4	23.1		11.8		6.3
CG.A pghpf 2.4	64.37	34.64	17.32	8.99		7.72		12.5
CG.A NPB2.3	36.4	20.7	9.6	4.4		2.6		1.6
MG.A pghpf 2.4	162.09	135.97	93.65	59.25		39.31		29.46
MG.A NPB2.3	52.7	30.0	15.0	7.6		4.0		2.1



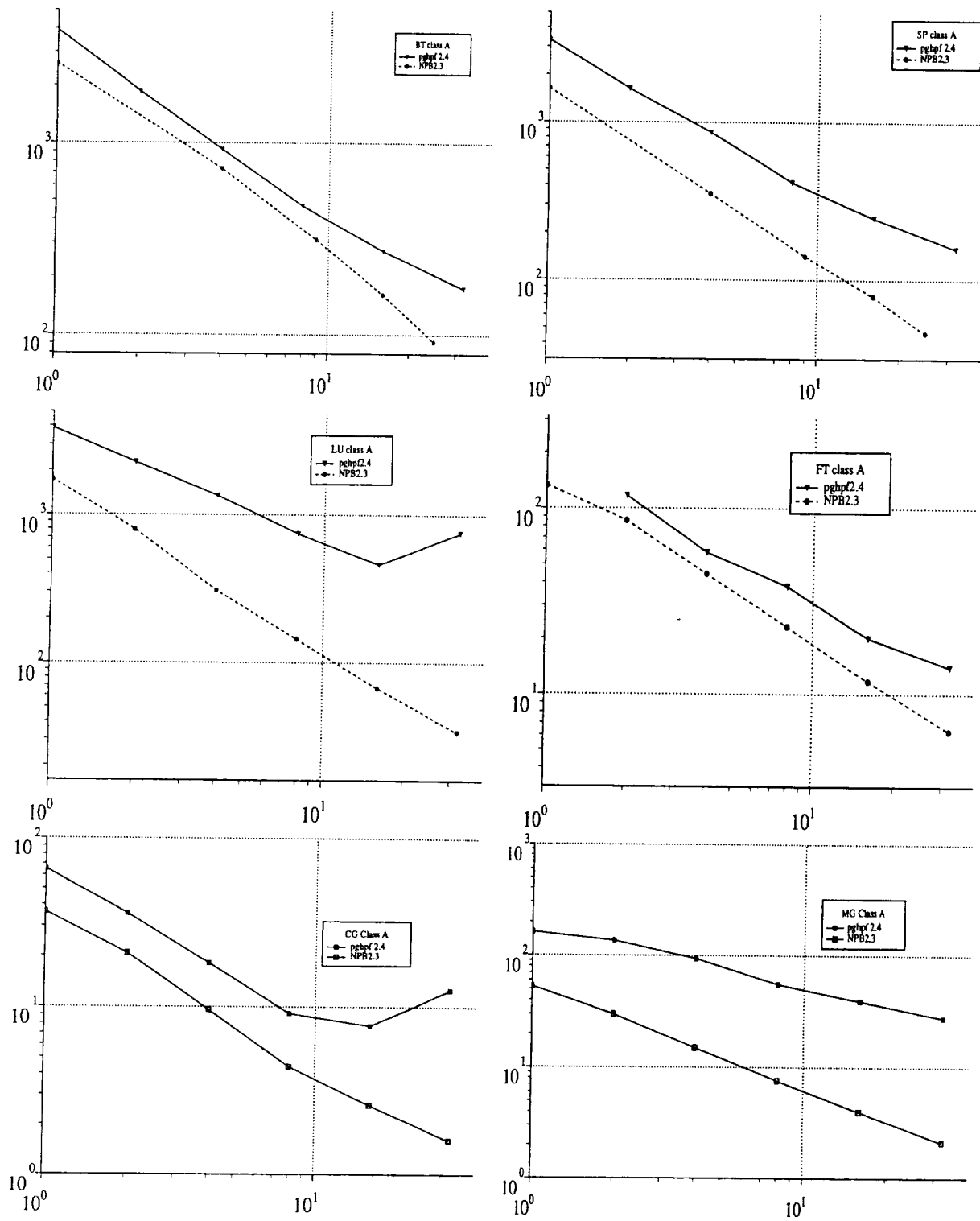


FIGURE 10. HPF versus MPI time for class A on SGI Origin 2000

## 6. Related Work and Conclusions

NPB are well recognized benchmarks for testing parallelizing compilers, parallel hardware and parallelization tools [1],[11],[13]. These benchmarks contain important kernels of aerophysics applications and may be used for early validation of various approach to development of high performance CFD codes.

Performance results of HPF implementation of “pencil and paper” NPB specifications submitted by APR and Portland Group are reported in [13], see also [www.apri.com/apr\\_nasbench.html](http://www.apri.com/apr_nasbench.html) and [www.pggroup.com/npb\\_results.html](http://www.pggroup.com/npb_results.html). The compiler vendors know the implementation of operations with distributed arrays and may be implicitly they have an HPF performance model. In some cases they use intrinsic customized HPF functions. It allows some `pghpf` compiled benchmarks to outperform hand-written MPI versions of NPB on CRAY T3D and CRAY T3E. Neither implementation has a version of LU benchmark. In APR’s implementation of MG a proprietary HPF directives set is used. The Portland Group FT implementation uses some HPF intrinsic functions customized for the benchmark.

The portability and scalability of HPF programs are studied in [11]. EP, FT and MG are used for comparison of a number of compilers, MPI and ZPL (a data parallel language developed at the University of Washington) implementations. One of the conclusions is that a consistent HPF performance model is important for scalability and portability of HPF programs. In the paper they regret: “Unfortunately, a portable HPF version of these (NPB) benchmarks is not available ...” and we hope that our paper provides a solution to the problem.

Problems of analysis and code generation for data parallel program discussed in [1]. As an solution the authors developed an integer-set framework and implemented it in dHPF environment. The framework was tested and profiled with SP, BT and LU.

A development of a large parallel application in an HPF programming paradigm called Fx is reported in [14]. The authors showed that an air pollution model Airshild fits into HPF programming paradigm and a good performance can be achieved on up to 64 processors of Cray T3D and Cray T3E. They also showed that the performance on different machines and different number of nodes can be modeled in a simple way.

An HPF implementation of reservoir simulation is reported in [6]. Two compiler

were compared and good scalability results were achieved on a number of platforms. Some other codes are used for testing of HPF compiler performance as well: CG 2D solver and Shallow Water code from NCAR: [www.digital.com/info/hpc/fortranS](http://www.digital.com/info/hpc/fortranS).

HPF gives a user a high-level programming language constructs for expressing parallelism existed in a sequential code. It allows to port a sequential code to a parallel environment with a moderate effort and results in a well structured parallel program. The machine architecture can be accounted for by using appropriate lower level message passing library as specified by `-Mmpi`, `-Msmp` or `-Mrmp` flags to `pghpf` compiler and requires a minimal effort from the user.

The hiding of distributed array handling results in uncertainty of the overhead of primitive operations with distributed arrays. Currently there is no HPF language constructs which can convey this overhead to the user. For example, data movement between processors can not be expressed in terms of HPF language. The problem is softened by `pghpf` compiler directives `-Minfo` and `-Mkeepftn` as well as by `pgprof` ability to show message size and number. A clear performance model of handling distributed arrays would allow the user to steer the code to a better performance.

The HPF model of parallelism appears to be adequate for expressing parallelism existed in BT, SP and FT with one exception. Due to inability of HPF organize pipelined computations an extra 3D array redistribution were required in each of these benchmarks. The concurrency regions of LU benchmark are planes normal to the grid diagonal and a nontrivial code modifications were required to express the parallelism.


At the current level of HPF compiler maturity it generates code which runs about 2 times slower on a single processor than the original serial code. On multiple processors the code speeds up almost linearly until the point where the redistribution creates a significant overhead. We have plans to implement ARC3D code in HPF and evaluate performance and portability of the benchmarks compiled with other HPF compilers.

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